United States Department of Agriculture





Economic Research Service

Technical Bulletin Number 1918

February 2008

# **Equilibrium Displacement Mathematical Programming Models**

Methodology and a Model of the U.S. Agricultural Sector

**David H. Harrington and Robert Dubman** 



Visit Ou

### **Visit Our Website To Learn More!**

You can find additional information about ERS publications, databases, and other products at our website.

## www.ers.usda.gov

## National Agricultural Library Cataloging Record:

Harrington, David H.

Equilibrium displacement mathematical programming models : methodology and a model of the U.S. agricultural sector.

(Technical bulletin (United States. Dept. of Agriculture); no. 1918)

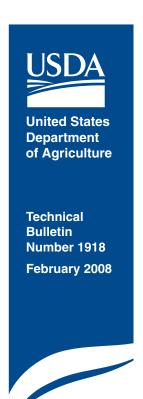
- 1. Programming (Mathematics).
- 2. Agriculture—Economic aspects—United States—Mathematical models.
- 3. Agriculture—Economic aspects—United States—Computer programs.
- Agriculture and state—United States.
- I. Dubman, Robert.
- II. United States. Dept. of Agriculture. Economic Research Service. III. Title.

QA402.5

Photo credit: PhotoDisc.

The U.S. Department of Agriculture (USDA) prohibits discrimination in all its programs and activities on the basis of race, color, national origin, age, disability, and, where applicable, sex, marital status, familial status, parental status, religion, sexual orientation, genetic information, political beliefs, reprisal, or because all or a part of an individual's income is derived from any public assistance program. (Not all prohibited bases apply to all programs.) Persons with disabilities who require alternative means for communication of program information (Braille, large print, audiotape, etc.) should contact USDA's TARGET Center at (202) 720-2600 (voice and TDD).

To file a complaint of discrimination write to USDA, Director, Office of Civil Rights, 1400 Independence Avenue, S.W., Washington, D.C. 20250-9410 or call (800) 795-3272 (voice) or (202) 720-6382 (TDD). USDA is an equal opportunity provider and employer.





www.ers.usda.gov

## Equilibrium Displacement Mathematical Programming Models

Methodology and a Model of the U.S. Agricultural Sector

**David H. Harrington and Robert Dubman** 

#### **Abstract**

The objective of this research is to extend and generalize the equilibrium displacement methodology by combining it with mathematical programming methods and existing knowledge of farm sector relationships to develop sectoral adjustment models that can operate in pure competition, monopoly/monopsony, or mixed-competition. A model of the U.S. agricultural sector at the national aggregate level is presented to illustrate the methods. An appendix contains a user's manual describing the operation of the model. Further appendices contain documentation of the structure of the spreadsheets, the programming tableau, and the SAS solution program.

**Keywords:** Equilibrium displacement models, mathematical programming, positive mathematical programming, U.S. agricultural sector, U.S. farm programs, direct payments, counter-cyclical payments, loan deficiency payments, marketing loan gains, conservation reserve program, wetlands reserve program, crop insurance

#### **Contents**

Summaryiv
Introduction
EDMP Methodology2Review of Literature2Theoretical Development3The EDMP Formulation5
Modeling the Supply Side
Modeling the Demand Side
Modeling Agricultural Policies and Programs11Payment Bases11Decoupled Payments11Counter-Cyclical Payments11Loan Deficiency Payments and Marketing Loan Gains12Conservation Reserve, Wetlands Reserve, and Grassland13Reserve Programs13Working Lands Conservation Programs14Crop Insurance Subsidies14Superseded Agricultural Programs15
Model Calibration
What Do Gradients Mean?
Structure of the Model.18Commodities.18Specified Resources18Specified Purchasable Inputs19Processes.19Agricultural Policies and Programs20
Solving the Model
Supply Parameters
Implicit Acreage- and Supply-Response Elasticities
Demand Parameters
Government Program Parameters30
Post-Optimal Calculations of Performance Variables32Net Farm Income and Net Cash Flow32Government Budgetary Exposure33Consumer and Producer Surpluses33Commodity Cash Incomes, Expenses, and Margins34

References	. 36
Appendix I: User's Manual	. 39
Appendix II: The SAS Excel Link Program	. 45
Appendix III: Model Spreadsheets.	. 53

Appendix III model spreadsheets are accessible by contacting David Harrington, 202-694-5571, davidh@ers.usda.gov